The High-Pressure Structural Evolution of Olivine along the Forsterite–Fayalite Join

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Abstract: Structural refinements from single-crystal X-ray diffraction data are reported for olivine with a composition of Fo100 (forsterite Mg2SiO4, synthetic), Fo80 and Fo62 (~Mg1.6Fe0.4SiO4 and ~Mg1.24Fe0.76SiO4, both natural) at room temperature and high pressure to ~8 GPa. The new results, along with data from the literature on Fo0 (fayalite Fe2SiO4), were used to investigate the previously reported structural mechanisms which caused small variations of olivine bulk modulus with increasing Fe content. For all the investigated compositions, the M2 crystallographic site, with its bonding configuration and its larger polyhedral volume, was observed to control the compression mechanisms in olivine. From Fo100 to Fo0, the compression rates for M2–O and M1–O bond lengths were observed to control the relative polyhedral volumes, resulting in a less-compressible M1O6 polyhedral volume, likely causing the slight increase in bulk modulus with increasing Fe content.

Keywords: olivine; forsterite; fayalite; crystal structure; high pressure; X-ray diffraction

1. Introduction

In order to understand the formation and evolution of the solid Earth, a precise knowledge of the elastic properties (e.g., bulk and shear modulus) of minerals present in the Earth’s interior at high pressures and high temperatures is necessary. These data are the basis for interpreting seismological profiles needed to determine the structure and composition of the Earth’s inaccessible interior (e.g., [1]). Olivine is the most abundant mineral in the upper mantle (51–60%; [2]) extending from the base of the crust to approximately 410 km. In natural systems, olivine forms a solid solution between two Mg and Fe end members, namely Mg2SiO4 forsterite (Fo) and Fe2SiO4 fayalite (Fa). At depths greater than 410 km, olivine is no longer stable and transforms to its high-pressure polymorph wadsleyite (β-olivine). This transformation is the cause of the 410 km seismic discontinuity that separates the upper mantle from the deeper transition zone (e.g., [3]). The exact pressure of this transition is a function of the Fe content of the system at a particular temperature (see [4] and references therein). Therefore, to understand the structure and composition of the mantle, and consequently global dynamics, accurate knowledge of the evolution of the elastic properties of olivine as a function of pressure and chemical composition is required.

The crystal structure of olivine (Pbnm space group) can be described as an expanded and distorted hexagonally close-packed (hcp) array of oxygen anions stacked along the a axis (e.g., [5,6]). Si cations
are located at tetrahedral sites, whereas Mg and Fe are disordered in two distinct octahedral sites, with the M1 polyhedron being smaller and more distorted than the M2 polyhedron (Figure 1).

Figure 1. Crystal structure of olivine plotted down the a axis. The b axis is plotted vertically (positive direction upwards), whereas the c axis is plotted horizontally (positive direction towards left). Atomic sites M2, M1, and Si are highlighted. The black rectangle represents the unit cell.

Many studies have been conducted in the past four decades in order to determine the elastic properties of olivine (e.g., the bulk modulus) as a function of pressure and composition (see [7–22]). However, the results of these studies have shown significant scattering. Nestola et al. [18] conducted a systematic study of the elastic properties of the Mg-rich side of the forsterite–fayalite join, which is relevant for mantle compositions. Importantly, this study illustrated that the isothermal bulk modulus (\(K_{\text{T0}}\)) and its first pressure derivative (\(K'\)) do not vary significantly between Fo92 to Fo0, thus a single equation of state was determined for the entire compositional range with \(K_{\text{T0}} = 124.7(9)\) GPa and \(K' = 5.3(3)\). More recently, Angel et al. [21] reviewed all available single-crystal data from the literature and constrained the elastic properties and pressure–volume–temperature equation of state (EoS) of mantle-composition olivine. For an olivine with Fo92–90 composition, these authors provided a \(K_{\text{T0}} = 126.3(2)\) GPa and \(K' = 4.54(6)\). On the Fe-rich side of the forsterite–fayalite join, Hazen [7] determined a \(K_{\text{T0}}\) of 113 GPa (\(K'\) fixed to 4) for a synthetic fayalite. More recently, Speziale et al. [16] used Brillouin scattering to determine the single-crystal elastic constants of a Fe-rich olivine \((\text{Fe}_{0.94}\text{Mn}_{0.06})_2\text{SiO}_4\) and provided an adiabatic bulk modulus (\(K_{\text{ad}}\)) of 134 GPa, which corresponds to a \(K_{\text{T0}}\) of about 135 GPa. The bulk modulus of Speziale et al. [16] is considered to be more accurate than the value obtained by Hazen [7], given the pioneering technology used more than 40 years ago in the latter study. In fact, a very recent work using synchrotron light in a multi-anvil apparatus [22] reported bulk moduli of 131.4 GPa for Fo85, 132.1 for Fo95, 136.3 for Fo18, and 134.8 for Fo0, in agreement with Speziale et al. [16]. These data confirmed that increasing the fraction of Fe in olivine stiffens its structure and increases the bulk modulus, possibly not following a linear trend. However, the reasons for this trend still require further understanding.

Crystallographic studies can provide insights into the nature of interatomic forces and compression mechanisms that control mineral elasticity. This is especially true with regards to Mg-rich olivine that, as mentioned above, displays almost no bulk modulus variation along a large compositional variability.
from Fo100 to Fo62 [18]. Therefore, it is crucial to understand the factors controlling its compression mechanisms. Finkelstein et al. [19] and Zhang et al. [20] recently investigated the crystal structure evolution of olivine end members Fo and Fa, respectively. However, a systematic study describing the structural evolution of olivine as a function of pressure and chemical composition is still lacking.

This study reports structural refinements from single-crystal X-ray diffraction data obtained on olivines with composition Fo100 (synthetic), Fo80, and Fo62 (natural) collected at room temperature and high pressure up to approximately 8 GPa. The new results, along with data from the literature on Fo90, are used to discuss and clarify the effect of Mg/Fe substitution on the structural deformation mechanisms occurring along the forsterite–fayalite join, relevant to upper-mantle compositions. In particular, this study focused on which structural mechanisms, at the atomic scale, can cause the very small variations of bulk modulus and its first pressure derivative that have been previously reported [18].

2. Materials and Methods

Three olivine single crystals (Fo100, Fo80, and Fo62) were investigated by single-crystal X-ray diffraction. Twin- and inclusion-free crystals for each composition, with typical dimensions <100 μm, were selected based on their sharp diffraction peaks. The Fo100 sample is a pure forsterite crystal that was synthesized in an experiment at room pressure and 1600 °C described in Smyth et al. [23]. The Fo80 and Fo62 specimens are natural crystals from the volcanic rocks of the Boseti Complex, Main Ethiopian Rift [24]. In detail, the two Fe-bearing olivines are samples from transitional alkaline basalts (BO 321) and strongly porphyritic basalts (BO 335), respectively (see Princivalle and Secco [24]). Single-crystal X-ray diffraction results and electron microprobe analyses were reported by Princivalle and Secco [24], and in the more recent study of Nestola et al. [18].

The cation distributions in terms of Mg and Fe reported by [24] for Fo80 and Fo62 are the following:

Fo80 (sample BO 321): M1 (Mg0.80, Fe0.20); M2 (Mg0.81, Fe0.19);
Fo62 (sample BO 335): M1 (Mg0.59, Fe0.40); M2 (Mg0.61, Fe0.38).

Olivine single crystals were loaded in an ETH-type diamond-anvil cell (DAC) to determine the evolution of their crystal structure at pressures up to ~8 GPa. High-pressure experiments were conducted separately for each composition, following the procedure described in Nestola et al. [18]. In particular, the samples were loaded on pre-indented T301 steel foil gaskets with holes of approximately 250 μm. A methanol:ethanol:water solution (in 16:3:1 ratio) was employed as the pressure-transmitting medium, which provides hydrostatic conditions up to ≈9.5 GPa [25,26], covering the pressure range investigated in this study. Pressures were determined by measuring the fluorescence of ruby chips [27], which were loaded in the sample chamber along with the olivine crystal.

Unit-cell parameters and intensity data (for structural refinements) were measured at nine different pressures up to approximately 8 GPa for forsterite (Fo100), and at seven different pressures up to ~7.7 and 8.3 GPa for Fo80 and Fo62, respectively. The measurements were carried out using a STOE STADI4 four-circle diffractometer (monochromatized Mo Kα radiation) (STOE & Cie GmbH, Darmstadt, Germany) equipped with an Oxford Diffraction CCD detector, with a sample–detector distance of 60 mm. Diffraction data were collected up to 2θ max = 60° using an exposure time of 60 s/frame and an ω-scan of 0.2° in order to obtain coverage of the full reciprocal sphere and the highest possible precision in the unit-cell parameters determination. The Crystals Red program (Oxford Diffraction) was used to integrate the intensity data, applying the Lorentz–polarization correction. The absorption correction for the crystal, DAC, and gasket shadowing was performed using Absorb 6.0 [28] and X-Shape [29]. Weighted structural isotropic refinements were performed using the SHELXL-97 software [30], starting from the atomic coordinates of Fujino et al. [31] in the Pbnm space group. No violation of the reflection conditions for this space group were observed to the maximum pressure reached for all the samples.
3. Results

Unit-cell parameters and structure refinement results are reported in Table 1, whereas bond lengths and polyhedral data are reported in Table S1 in the Supplementary Material. The atomic coordinates of all samples at all pressures are provided as CIF files in the Supplementary Material.

### Table 1. Unit-cell parameters and structure refinement results for the olivine crystals studied here.

<table>
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<th>Fo&lt;sub&gt;100&lt;/sub&gt;Fa&lt;sub&gt;0&lt;/sub&gt;</th>
<th>P (GPa)</th>
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<th>1.22(5)</th>
<th>2.04(5)</th>
<th>2.67(5)</th>
<th>3.28(5)</th>
<th>4.82(5)</th>
<th>6.29(5)</th>
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<td>4.750(3)</td>
<td>4.741(3)</td>
<td>4.734(4)</td>
<td>4.732(4)</td>
<td>4.725(4)</td>
<td>4.714(3)</td>
<td>4.704(2)</td>
<td>4.700(3)</td>
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<tr>
<td>c (Å)</td>
<td>5.982(6)</td>
<td>5.962(4)</td>
<td>5.946(4)</td>
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<td>287.8(3)</td>
<td>286.1(3)</td>
<td>284.8(4)</td>
<td>283.6(2)</td>
<td>280.7(4)</td>
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<td>214</td>
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<td>R&lt;sub&gt;wp&lt;/sub&gt; (%)</td>
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Bulk modulus, \(K_{T0} = 124.4\) GPa
First pressure derivative, \(K' = 4.9\)

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<th>Fo&lt;sub&gt;80&lt;/sub&gt;Fa&lt;sub&gt;20&lt;/sub&gt;</th>
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<td>b (Å)</td>
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<td>282.9(4)</td>
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<td>R&lt;sub&gt;wp&lt;/sub&gt; (%)</td>
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Bulk modulus, \(K_{T0} = 124.7(3)\) GPa
First pressure derivative, \(K' = 5.4(2)\)

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<th>Fo&lt;sub&gt;62&lt;/sub&gt;Fa&lt;sub&gt;38&lt;/sub&gt;</th>
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<th>0.76(5)</th>
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<th>2.86(5)</th>
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<td>b (Å)</td>
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<td>10.296(4)</td>
<td>10.283(4)</td>
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Bulk modulus, \(K_{T0} = 126.6(4)\) GPa
First pressure derivative, \(K' = 5.2(1)\)

Note: Bulk moduli and first pressure derivatives from [18].

The evolution of the M2 and M1 polyhedral volumes (plotted as \(V/V_0\)) with pressure is shown in Figure 2. All samples displayed similar behaviour, where the M2 polyhedron compressed more than M1. Thus, the evolution of the M2 polyhedron volume is likely the main factor influencing the compression mechanism in olivine.
Figure 2. The evolution of normalized $V/V_0$ for M2 and M1 polyhedra: (a) $\text{Fo}_{100}$; (b) $\text{Fo}_{80}$; (c) $\text{Fo}_{62}$.
The polyhedral volume compressibility, expressed as $\beta = [V - V_0/V_0] / \Delta P$, can be used to compare the effect of composition (Fe content) on the compressional behaviour of olivine. Based on data reported in Table S1, the values obtained for M2 and M1 polyhedra, respectively, are:

- $\text{Fo}_{100}$: $\beta = -0.0079(5)$ and $-0.0066(4)$ GPa$^{-1}$,
- $\text{Fo}_{80}$: $\beta = -0.0073(5)$ and $-0.0065(4)$ GPa$^{-1}$,
- $\text{Fo}_{62}$: $\beta = -0.0072(5)$ and $-0.0056(4)$ GPa$^{-1}$.

These values seem to indicate that $\text{Fo}_{62}$ is the stiffest structure and $\text{Fo}_{100}$ is the most compressible. However, when considering the associated uncertainties, the observed differences of $\beta$ between $\text{Fo}_{100}$ and $\text{Fo}_{62}$ are negligible over the large compositional range. The polyhedral volume of the unique tetrahedral site does not present any significant variations over the pressure range investigated for all compositions, indicating that the Si tetrahedron is a rigid unit, as commonly observed in silicate minerals (e.g., [20]).

The volume distortions of the M2 and M1 polyhedra were calculated using the IVTON software [32] as $[V_i - V_p] / V_i$, where $V_i$ is the volume of the ideal polyhedron and $V_p$ the volume of the coordination polyhedron. These data are reported in Table S1. In general, the M1 polyhedron in olivine is smaller and more distorted than the M2 [5,6]. However, at room pressure, the M2 and M1 octahedra showed an almost identical distortion for $\text{Fo}_{100}$ and $\text{Fo}_{80}$. In contrast, both the M2 and M1 octahedra in $\text{Fo}_{62}$ were more distorted (between 18% and 25%) when compared to $\text{Fo}_{100}$ and $\text{Fo}_{80}$. This behaviour may explain the compressibility change toward higher bulk moduli in more Fe-rich compositions. Instead, the Si tetrahedron was again the most regular, regardless of the composition considered.

The M2–O and M1–O bond lengths are reported in Table S1 and their evolution as a function of pressure is displayed in Figures 3 and 4.

As expected, from the behaviour of the polyhedral volumes, the M2–O average values exhibited the largest variation in pressure, with the T–O average distances essentially unchanged over the entire pressure range. This observation further confirms that the M2 crystallographic site, with its bonding configuration, controls the compressibility of olivine. However, it is not clear whether a different compression trend was observed over the compositional range studied in this work. In fact, by normalizing the single bond length compressions (using a simple linear calculation, where the difference between the initial and final bond lengths values are normalized over the pressure range investigated, providing the compression in Å/GPa), the M–O differences obtained for $\text{Fo}_{100}$ to $\text{Fo}_{62}$ were modest, if not negligible (Table 2).

<table>
<thead>
<tr>
<th></th>
<th>$\text{Fo}_{100}$</th>
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<td>M2–O1</td>
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<td>0.009</td>
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<td>M2–O2</td>
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<td>0.006</td>
<td>0.006</td>
<td>0.007</td>
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<td>M2–O3i × 2</td>
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<td>0.012</td>
<td>0.010</td>
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<td>M2–O3s × 2</td>
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<td>Mean compression rate (Å/GPa)</td>
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Values were calculated from the data reported in Table S1 and from the CIF files deposited by Zhang et al. [20] for $\text{Fo}_0$ (between 3.9 and 12.3 GPa, see text). All data are normalized to ensure a reliable comparison. Uncertainties are $\leq 0.002$ Å/GPa for M2–O lengths and $\leq 0.001$ Å/GPa for M1–O lengths.
Figure 3. M2–O bond distance versus pressure for samples (a) Fo100, (b) Fo80, and (c) Fo62. Symbols: red squares, M2O1; black circle, M2O2; blue upward triangle, M2–O3l; grey downward triangle, M2–O3s. Lines connect points over the investigated pressure range for a particular bond distance and only serve as guides.
Figure 4. M1–O bond distance versus pressure for samples (a) Fo100, (b) Fo80, and (c) Fo62. Symbols: red squares, M1O1; black circles, M1O2; blue upward triangles, M1–O3. Lines connect points over the investigated pressure range for a particular bond distance and only serve as guides.
4. Discussion

Before discussing the high-pressure structural variation as a function of composition, it is important to note that no significant bulk modulus variations were observed in the compositional range investigated by Nestola et al. [18], that is, between Fo_{92} and Fo_{62}. However, the data by Nestola et al. [18] showed a possible tendency to develop a stiffer structure for Fo_{62}, with slightly higher linear moduli along the crystallographic a and c axes, while no differences were observed along the b axis. Combining the small variations along these axes resulted in a slightly higher bulk modulus for Fo_{62}, closer to 127 GPa [18].

The results presented here for Mg-rich olivines can be interpreted with the most recent data of Bejina et al. [22] and Speziale et al. [16] on Fe-rich olivines. These data indicate that increasing the Fe content along the forsterite–fayalite join causes a slight but significant increase in the bulk modulus of olivine. The total increase from Fo_{100} to Fo_{0} could be quantified as approximately 9%. However, the increment with Fe content of $K'_{T0}$ was non-linear: from Fo_{100} to approximately Fo_{60}, the bulk modulus was almost constant with values between 124 and 126 GPa, whereas from Fo_{60} to Fo_{18} a large variation from ~126 to 136 GPa was observed. No significant variations were detected between Fo_{18} and Fo_{0}. Nevertheless, $K'$ remained nearly constant over the entire compositional Fo–Fa join, with a value close to 5. This value was calculated based on the data of Nestola et al. [18] and Speziale et al. [16], as all other studies in the literature fixed the $K'$ to 4. As mentioned above, it appears that two plateaus for the Mg-rich and the Fe-rich portions of the join are present [22] (see their Figure 8). In order to explain these bulk modulus differences, it would be useful to compare structural data for olivine within this compositional range, but unfortunately the only recent data on single crystals are those presented in this study and in Zhang et al. [20] on fayalite. The pioneering work of Hazen [7] and Kudoh and Takeuchi [9] were not considered in this study, as their data were collected when high-pressure protocols were at their initial stages, three to four decades ago. Since the bulk modulus does not show any significant variations between Fo_{20} and Fo_{0}, the structural data for Fo_{100}, Fo_{80}, Fo_{62} and Fo_{0} can be compared. Zhang et al. [20] investigated Fo_{0} up to 31 GPa; however, only data between 3.7 and 12.3 GPa were considered, which correspond to a pressure range of 8.4 GPa (similar to what was investigated in this study). A first direct comparison with fayalite can be done relative to the compressions of the M1–O and M2–O bond lengths. As observed for Mg-rich compositions, M2–O lengths were the most compressible also in fayalite. Thus, the main deformation mechanism in olivine is driven by the M2 bonding configuration. However, the mean compression rate for the M2–O bond lengths was identical between the two end-members, with values of 0.006, 0.005, 0.006, and 0.006 Å/GPa for Fo_{100}, Fo_{80}, Fo_{62}, and Fo_{0}, respectively (values obtained summing the single compression rates reported in Table 2 and divided by the number of bond distances). The same calculation performed for the M1–O bond lengths provides compression rates of 0.005, 0.005, 0.004, and 0.004 Å/GPa for Fo_{100}, Fo_{80}, Fo_{62}, and Fo_{0}, respectively. The compression rate for M2–O and M1–O bond lengths controls the relative polyhedral volumes, resulting in a less-compressible M1 polyhedron from Fo_{100} to Fo_{0}, causing a slight increase in the bulk modulus with increasing Fe content. These small structural variations can also explain the almost constant first pressure derivative of the bulk modulus along the forsterite–fayalite join, indicating a very similar structural compression motif.

**Supplementary Materials:** The following are available online at [http://www.mdpi.com/2075-163X/9/12/790/s1](http://www.mdpi.com/2075-163X/9/12/790/s1), Table S1: Bond lengths and polyhedral data for the olivine crystals studied here.

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