

I. (20) Define the following terms:

A. Dispersion

Index of refraction is a function of wavelength (color).

B. Indicatrix

An ellipsoidal figure representing the indices of refraction for the various vibration directions for light in a crystal.

C. Diffraction

The coherent scattering of a wave from a periodic array of scatterers.

D. Pleochroism

Absorption of light is a function of direction in a crystal.

E. Liquidus

The line on a temperature-composition phase diagram above which the system is completely liquid.

II. (15) I want to synthesize a sample of wadsleyite with a composition (formula) of  $Mg_{1.70}Fe_{0.30}SiO_4$  by mixing together powdered oxide reagents of  $SiO_2$ ,  $MgO$ , and  $FeO$ . (Oxide molecular weights are 60.086, 40.312, and 71.846 g, respectively as listed.) If I need a total of one gram (1000 mg) of starting material, how many milligrams of each oxide do I need to weigh out and mix together? (Hint: calculate weight percentages first.)

Oxide	MolWt Oxide	Moles per form.	<u>g/form</u>	<u>wt%</u>	<u>mg/g</u>
$SiO_2$	60.086	1.000	60.086	40.012	400.12
$MgO$	40.312	1.700	68.530	45.635	456.35
$FeO$	71.846	0.300	<u>21.554</u>	<u>14.353</u>	<u>143.53</u>
			150.170	100.00	1000.00

III. A. (10) Periclase ( $MgO$ ), is a relatively rare metamorphic alteration product of dolomite, but is also believed to be a significant constituent of the lower mantle co-existing with bridgmanite. The crystal structure of periclase is cubic with a cell edge of 4.21Å and Z of 4 for pure  $MgO$ .  $MgO$  has a molecular weight of 40.3114g. Calculate the density of periclase.

$$\rho = z \text{ FW} / A V$$

$$\rho = 4 \cdot 40.3114 / .6023 \times (4.21)^3$$

$$\rho = 3.588 \text{ g/cm}^3$$

III. B. (10) The index of refraction of periclase is 1.74. What is the speed of light in periclase?

$$V = c/n$$

$$V = 3.0 \times 10^8 / 1.74$$

$$V = 1.724 \times 10^8 \text{ m/s}$$

III. C. (10) Calculate the  $2\theta$  angle for Cu  $K\alpha$  radiation ( $\lambda = 1.5405\text{\AA}$ ) for the (2 0 0) and (111) X-ray diffraction peaks of periclase ( $a = 4.212 \text{ \AA}$ ).

$$d_{200} = a / 2$$
$$d_{200} = 2.106$$

$$2\theta = 2 \sin^{-1} \lambda/2d$$
$$2\theta = 2 \sin^{-1} 1.5405/4.212$$
$$2\theta = 42.91^\circ$$

$$d_{111} = a / 1.732$$
$$d_{111} = 2.432$$

$$2\theta = 2 \sin^{-1} 1.5405/4.864$$
$$2\theta = 36.93^\circ$$

IV. (15) Siderite,  $\text{FeCO}_3$ , is trigonal and uniaxial negative. Its two indices of refraction are 1.575 and 1.782.

- A. A laser beam enters a siderite crystal propagating in the  $c$ -direction and vibrating in the  $a$ - $b$  plane. Do you expect this light beam to experience strong birefringence?

No

Why? looking down the optic axis

- B. The laser beam enters the crystal propagating parallel to the  $a$ -axis and vibrating in the  $a$ - $c$  plane. Do you expect this beam to experience strong birefringence?

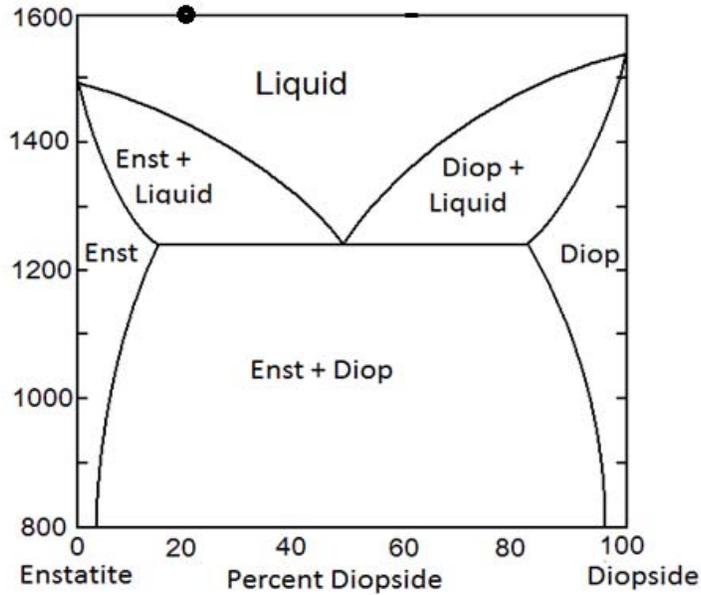
Yes

Why? looking perpendicular to optic axis

- C. In this latter orientation (propagating parallel to  $a$  and vibrating in the  $a$ - $c$  plane), do you expect to see strong pleochroism? Yes

Why? Fe-bearing and looking perpendicular to optic axis

V. (20) Below is a simplified melting (T-X) diagram for enstatite ( $Mg_2Si_2O_6$ ) – diopside ( $CaMgSi_2O_6$ ). There is limited crystalline solution between the end member. Starting with a liquid composition 80% enstatite and 20% diopside at 1600°C (dot) answer the following questions based on the diagram assuming perfect equilibrium between crystals and solid:



- A. At what temperature do the first crystals form? 1450°
- B. How many phases are present at 1300°C? 2
- C. At what temperature does the last liquid disappear? 1240°
- D. What is the composition of the last liquid to crystallize? En50Di50
- E. How many phases are present at 1100°C? 2
- F. What is the composition of the enstatite phase at 1100°C? En90Di10
- G. What is the composition of the diopside phase at 1100°C? En12Di88