Erratum

Single-crystal elasticity of wadsleyites, $\beta$-Mg$_2$SiO$_4$, containing 0.37–1.66 wt.% H$_2$O

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Abstract

The presence of hydrogen can affect elastic properties and seismic velocities of minerals in the Earth’s upper mantle. In this study, the second-order elastic constants of hydrous wadsleyites containing 0.37, 0.84, and 1.66 wt.% H$_2$O were determined by Brillouin scattering at ambient conditions. Measurements were performed on at least three independent crystal planes for each composition. The aggregate bulk modulus, $K_{S0}$, and shear modulus, $G_0$, were calculated using VRH (Voigt–Reuss–Hill) averages. The results are: $K_{S0} = 165.4(9)$ GPa, $G_0 = 108.6(6)$ GPa for wadsleyite with 0.37 wt.% H$_2$O; $K_{S0} = 160.3(7)$ GPa, $G_0 = 105.3(6)$ GPa for 0.84 wt.% H$_2$O; $K_{S0} = 149.2(6)$ GPa, $G_0 = 98.6(4)$ GPa for 1.66 wt.% H$_2$O. We find that the bulk and shear moduli of hydrous wadsleyites decrease linearly with water content according to the following relations (in GPa): $K_{S0} = 170.9(9) - 13.0(8)C_{H2O}$, $G_0 = 111.7(6) - 7.8(4)C_{H2O}$, where $C_{H2O}$ is the H$_2$O weight percentage. Compared with anhydrous wadsleyite, addition of 1 wt.% H$_2$O will lead to a 7.6% decrease in the bulk modulus, and a 7.0% decrease in the shear modulus. Using these results, we examine the velocity contrast between hydrous olivine and wadsleyite at ambient conditions for an Fe-free system assuming an H$_2$O partition coefficient between wadsleyite and olivine of 3. The velocity contrast in compressional and shear velocity between wadsleyite and olivine ranges from 12%–13% for an H$_2$O-free system to 7%–8% for wadsleyite containing 1.5 wt.% H$_2$O. Thus, the magnitude of the seismic velocity change at 410-km depth can be expected to be sensitive to the presence of H$_2$O in olivine polymorphs.

Keywords: Hydrous wadsleyite; Elasticity; Brillouin scattering; Velocity contrast; Transition zone

1. Introduction

Wadsleyite ($\beta$-Mg$_2$SiO$_4$) is the high-pressure polymorph of olivine that is expected to be a dominant mineral in the Earth’s mantle from 410 km to 520 km depth. Previous studies show that wadsleyite can incorporate variable amounts of water as structurally bound hydroxyl (OH), up to a maximum of 3.3 wt.% H$_2$O if every non-silicate oxygen site in the structure is protonated (Smyth, 1987, 1994). Wadsleyite has the greatest hydrogen storage capacity among the olivine polymorphs. At transition zone conditions (~15 GPa, 1400 °C), the water content of wadsleyite coexisting with hydrous melt is about 0.9 wt.% (Demouchy et al., 2005). Ringwoodite, which is the stable olivine polymorph from 520 km to 660 km depth, can also incorporate 2–3 wt.% H$_2$O below 1100 °C and up to ~0.3 wt.% H$_2$O at 1500–1600 °C (Kohlstedt et al., 1996; Ohtani et al., 2000). Thus, the Earth’s transition zone, which is dominated by ringwoodite and wadsleyite, could contain a large water reservoir perhaps even exceeding the mass of the hydrosphere (Smyth, 1994).

Small amounts of H$_2$O can strongly influence a number of important physical properties of mantle minerals. Hydration is...
expected to alter the thickness and depth of the olivine to wadsleyite phase transition (e.g., Wood, 1995; Chen et al., 2002; Smyth and Frost, 2002), promote partial melting (Hirschmann, 2006), and alter rheological and transport properties (Chen et al., 1998; Huang et al., 2005; Karato, 2006). Incorporation of H2O will also affect elastic properties (Jacobsen, 2006). Knowledge of the elastic properties of wadsleyite is crucial for interpreting seismic profiles and tomographic images of the mantle and identifying potential water-rich regions. To date, the elasticity of hydrous wadsleyite has been investigated only by static compression studies (Yusa and Inoue, 1997; Smyth et al., 2005; Holl et al., in press). Yusa and Inoue (1997) report that incorporation of 2.5 wt.% of H2O leads to a 15% reduction in the isothermal bulk modulus, K\textsubscript{T0}, for a fixed value of the pressure derivative, (∂K\textsubscript{T}/∂P)\textsubscript{T0}=K\textsubscript{T0}. However, static compression studies on various hydrous olivine polymorphs (Smyth et al., 2004, 2005; Manghnani et al., 2005; Holl et al., in press) show that incorporation of water may increase K\textsubscript{T0}. Furthermore, the shear modulus cannot be determined from static compression.

In this study, we use Brillouin scattering to determine the full elastic tensor of hydrous wadsleyite and place bounds on the bulk and shear moduli of polycrystalline aggregates. The variation of elastic moduli of wadsleyite as a function of H2O content was and shear moduli of polycrystalline aggregates. The variation of elastic moduli of wadsleyite as a function of H2O content was obtained by measuring three different compositions containing 0.37(4) wt.% H2O, 0.84(8) wt.% 1.66(17) wt.% H2O, respectively. The potential effect of hydration on the velocity contrast between olivine and wadsleyite is examined. Variations in aggregate elastic properties of olivine polymorphs are systematically evaluated as a function of phase, Fe content, and hydration.

2. Experimental details

2.1. Synthesis and characterization

Single crystals of hydrous wadsleyite, β-Mg\textsubscript{2}SiO\textsubscript{4}, were synthesized in the 1200-ton Hymag or Sumitomo multianvil presses at the Bayerisches Geoinstitut, Bayreuth, Germany. Starting materials consisted of mixed oxide powders; MgO plus SiO\textsubscript{2} with slight excess silica and water added as brucite, Mg(OH)\textsubscript{2}. Runs were carried out in welded platinum capsules at conditions of 14–16 GPa and 1200–1400 °C with heating durations of at least one hour and rapid quenching. Samples were selected for Brillouin scattering from runs WH833 (Jacobsen et al., 2005), SS0401 (Holl et al., in press), and a new synthesis run, WH2120.

Lattice parameters for representative crystals from each run (Table 1) were determined by single-crystal X-ray diffraction using eight-position centering of 15–20 low-angle reflections on either the Huber four-circle diffractometer in Bayreuth (samples WH833 and WH2120) or the Bruker P4 four-circle diffractometer in the Mineral Structures Laboratory at the University of Colorado (sample SS0401). For selected samples from WH833 and WH2120, additional energy dispersive single-crystal diffraction measurements were carried out at the X17C beamline of the National Synchrotron Light Source (Hu et al., 1993) to determine the orientations of polished platelets. For SS0401, selected orientations were determined at the University of Colorado.

Previous studies (Smyth et al., 1997; Kudoh and Inoue, 1999) have reported a monoclinic distortion in hydrous wadsleyite. The cause of monoclinic symmetry in hydrous wadsleyite remains unresolved, but it has been speculated to result from cation vacancy ordering (Smyth et al., 1997), stacking disorder of distinct structural modules (Kudoh and Inoue, 1999), or polysynthetic twinning (Holl et al., in press). Among six hydrous wadsleyite runs studied by Jacobsen et al. (2005), only samples with water contents greater than about 0.5 wt.% H2O displayed the monoclinic symmetry. In this study, samples from run WH833 are orthorhombic with average β=90.002(3)° (Jacobsen et al., 2005). Samples from run WH2120 display a slight monoclinic distortion with average β=90.044(5)°. Samples from run SS0401 display angles of up to 90.09(2)°. For the present Brillouin scattering measurements, these slight distortions are not considered and orthorhombic (Imma) symmetry is assumed.

2.2. Water contents

The concentration of hydroxyl (OH) in hydrous wadsleyite is commonly reported in wt.% H2O or parts per million by weight (ppm wt.), where 1 wt.% H2O=10,000 ppm wt. H2O. Estimating the water contents is problematic because an absolute calibration for OH specific to wadsleyite has not been established for either IR spectroscopic or secondary ion mass spectrometry (SIMS). Polarized Fourier transform infrared (FTIR) spectroscopy was used to estimate the water content of sample WH833 using the calibration of Libowitzky and Rossman (1997), resulting in 0.37 wt.% as the sum from polarized measurements with E∥a, E∥b, and E∥c (Jacobsen et al., 2005). Spectra for sample WH833 with E∥b are shown in Fig. 1. Polarized-IR spectra for samples WH2120 and SS0401 are also shown in Fig. 1, and illustrate the typical problem of using IR to study wadsleyite. Namely, the dominant absorption band pair at 3300–3400 cm\textsuperscript{-1} cannot be resolved because of the high water content (>0.5 wt.%) in these samples. The spectra in Fig. 1 were obtained from 30-micron thick plates, but the use of thinner plates measuring ~10 μm thickness for SS0401 also resulted in complete absorption at 3300–3400 cm\textsuperscript{-1}. Therefore, the relationship between the b/a axial ratio and estimated water content from Jacobsen et al. (2005) was used to calculate the water content of WH2120 and SS0401. This relationship, b/a=2.008+1.25×10\textsuperscript{-6}C\textsubscript{OH} (in ppm wt.) uses water contents from IR at lower concentrations and SIMS data at higher concentrations. The correlation uses b/a because the b axis of wadsleyite increases

Table 1

| H2O content and crystallographic data of hydrous wadsleyite samples |
|-----------------------------|-----------------------------|-----------------------------|
| WH833 \textsuperscript{a} | WH2120 | SS0401 \textsuperscript{b} |
| H2O (wt.%) | 0.37(4) | 0.84(8) | 1.66(17) |
| a (Å) | 5.6941(2) | 5.6888(6) | 5.6807(3) |
| b (Å) | 11.4597(3) | 11.4830(8) | 11.5243(6) |
| c (Å) | 8.2536(2) | 8.2523(6) | 8.2515(6) |
| V (Å\textsuperscript{3}) | 538.70(3) | 539.08(8) | 540.20(5) |
| ρ (g/cm\textsuperscript{3}) | 3.453(2) | 3.435(7) | 3.395(10) |


\textsuperscript{a} Lattice parameters of WH833 are from Jacobsen et al. (2005).

\textsuperscript{b} Lattice parameters of SS0401 are from Holl et al. (in press).
systematically with water content and the $a$ axis decreases systematically with increasing water content. Although there is also a clear positive volume of hydration (i.e. volume increases with water content), by using $b/a$ individual measurements are not subject to absolute uncertainty in the volume, which may vary from one diffractometer to another. The $b/a$ relationship results in 0.84 wt.% H$_2$O for sample WH2120 and 1.66 wt.% H$_2$O for SS0401. Water contents for all samples studied by Brillouin spectroscopy in this study are listed in Table 1. Because there is no absolute calibration for water in wadsleyite, we have chosen to use arbitrary 10% error bars in subsequent figures and in calculation of density.

2.3. Variation of density with water content

Measured unit cell volumes and water contents were used to calculate the variation of density (Fig. S1). A nominally anhydrous sample (WS3056) containing about 50 ppm wt. H$_2$O with $\rho_{\text{calc}} = 3.472(1)$ g/cm$^3$ from the study of Jacobsen et al. (2005) is used for comparison. This sample represents the least amount of water from attempts to synthesize wadsleyite without hydroxyl (Jacobsen et al., 2005). Formula weights were calculated according to the stoichiometry Mg$_{2-x}$H$_x$SiO$_4$, where $2x$ was determined as discussed in Section 2.2 and full Si occupancy is assumed. The decrease in density of wadsleyite at STP varies as:

$$\rho = 3.472(1) - 0.046(2) \times C_{\text{H}_2\text{O}}$$  \hspace{1cm} (1)$$

where density is given in g/cm$^3$ and $C_{\text{H}_2\text{O}}$ is the H$_2$O weight percentage.

2.4. Raman spectroscopy

Raman spectra were measured for all samples at ambient conditions. Up to 22 Raman modes were observed for a given sample (Fig. S2). The peak positions obtained for the sample with 1.66 wt.% H$_2$O are generally in good agreement with a previous study (Kleppe et al., 2001) which had a nearly identical water content. In the range 200–1100 cm$^{-1}$, most of modes show a subtle decrease in frequency with water content. Lattice mode frequencies typically decrease by $\sim$3 cm$^{-1}$ from nominally anhydrous wadsleyite to samples with 1.66 wt.% H$_2$O. We also observed three OH modes for each composition (Table S1). Compared with Kleppe et al. (2001), our OH modes occur at slightly lower frequencies. For the OH doublet at 3321 cm$^{-1}$ and 3582 cm$^{-1}$, the frequency increases by 7.4 cm$^{-1}$ and 8.8 cm$^{-1}$ respectively from 0.37 to 1.66 wt.% H$_2$O. The frequency increases by 2.6 cm$^{-1}$ for the 3582 cm$^{-1}$ mode over the range of water content. Thus, water has a weak but detectable effect on Raman frequencies, with lattice modes generally decreasing and OH modes increasing as a function of H$_2$O content.

2.5. Brillouin spectroscopy

All samples were double-side polished to thicknesses ranging from 30 µm to 200 µm. A large-opening diamond anvil cell was used to hold platelets that were less than 50 µm thick. Since all the experiments were performed at ambient conditions, no pressure was applied to the diamond cell. A special cell was designed to hold platelets thicker than 50 µm. This holder was...
made from a stainless steel gasket with a 1-mm hole in the center. The crystal platelet was loaded into the center of the gasket hole and sandwiched between two glass slides.

Brillouin spectra were measured in a forward scattering geometry at ambient conditions using a six-pass Sandercock tandem Fabry–Perot interferometer. The sample was probed using a solid state laser with a wavelength 532.15 nm and power of about 150 mW. For a symmetric scattering geometry, acoustic velocities are related to the measured Brillouin frequency shift $\Delta \nu_B$ by:

$$\nu = \frac{\Delta \nu_B \lambda_0}{2\sin(\theta/2)}$$

where $\nu$ is the acoustic velocity, $\lambda_0$ is the incident wavelength, $\theta$ is the external scattering angle (70° in this study). Further details of the Brillouin system are provided elsewhere (Speziale and Duffy, 2002).

For each platelet, we collected spectra at 10° steps in a total of 19 directions over a range of 180°. The average collection time ranged from 30 to 50 min per spectrum. Fig. 2 shows an example Brillouin spectrum of hydrous wadsleyite. One quasi-longitudinal and two quasi-transverse modes were observed in most directions. The three acoustic modes are usually clearly separated. All spectra had a high signal-to-noise ratio. The uncertainty of the measurement was within 0.5 to 1% of the measured velocities.

3. Results

Although some of our samples display a slightly monoclinic distortion which would require characterization of 13 elastic constants, the Brillouin data were fitted assuming orthorhombic symmetry because the angular deviation from 90° is small (see Section 2.1). In this case, nine independent elastic constants are needed to characterize each sample. The orientation of each platelet can be described by three Eulerian angles ($\theta$, $\phi$, $\chi$) that relate the laboratory coordinate system to the crystal coordinate system (Shimizu, 1995). The Eulerian angles together with an azimuthal angle determine the phonon propagation direction which can be expressed by the direction cosines, $n_i$. In total, there are $9 + 3k$ unknown parameters ($9$ elastic constants, $k$ platelets, $3k$ Eulerian angles). These were obtained by fitting the velocity data for all platelets of a given composition simultaneously using Christoffel’s equation (Every, 1980):

$$\det[C_{ijkl}n_i n_j - \rho \nu^2 \delta_{ik}] = 0$$

where, $\rho$ is the density, $\nu$ is the phonon velocity, $n_i$ are the direction cosines of the phonon propagation direction, and the
Some uncertainty is likely introduced due to the remounting of the assembly holding the crystal platelets between the X-ray and Brillouin measurement. In addition, covariance among the Eulerian angles for a given plane may also contribute to uncertainty in recovered orientations. Fig. 3 shows the experimentally obtained velocity data together with values calculated from the best fitting elastic constants for WH833 with 0.37 wt.% H$_2$O. For WH2021 and SS0401, results are presented in Fig. S3. The root-mean-square (RMS) deviation (Table S2) between measured and calculated acoustic velocities ranges from 39 m/s to 51 m/s. This indicates excellent agreement between the measured and calculated acoustic velocities.

In Fig. 4, variation of individual elastic moduli with water content is shown. Linear fits to the $C_{ij}$ values including nominally anhydrous compositions (Sawamoto et al., 1984; Zha et al., 1997) as a function of H$_2$O content are shown by the solid lines. Longitudinal moduli $C_{11}$, $C_{22}$, $C_{33}$, shear modulus, $C_{44}$, and off-diagonal modulus, $C_{23}$, display a well-defined linear decrease with H$_2$O content. Due largely to the difference between anhydrous elastic constants of Sawamoto et al. (1984) and Zha et al. (1997), the trends for $C_{55}$, $C_{66}$, $C_{12}$, and $C_{13}$ are less certain. $C_{23}$ is the elastic modulus most strongly affected by incorporation of water. It decrease 20% as water content increases from 0% to 1.66 wt.% H$_2$O. On the other hand, $C_{12}$ only shows a weak dependence on water content. The longitudinal ($C_{11}$, $C_{22}$, $C_{33}$) and shear ($C_{44}$, $C_{55}$, $C_{66}$) moduli all show similar decreases with water content.

The covariance matrix was calculated to evaluate the trade-off among recovered pairs of elastic constants (Press et al., 1988; Brown et al., 1989). In general, trade-off coefficients for longitudinal and shear moduli are small and indicate the elastic moduli are well-resolved. $C_{12}$ is the most poorly constrained elastic modulus. For sample WH833 (0.37 wt.% H$_2$O), $C_{12}$ shows strongest dependence on the value of $C_{11}$, $C_{22}$, $C_{33}$, and $C_{66}$. For sample WH2120 (0.84 wt.% H$_2$O), $C_{12}$ depends on the value of $C_{13}$, $C_{22}$, $C_{33}$ and $C_{66}$. The trade-off between $C_{11}$ and $C_{66}$, $C_{13}$ and $C_{66}$ for sample WH833, $C_{11}$ and $C_{12}$, $C_{23}$ and $C_{66}$, $C_{23}$ and $C_{13}$ for sample WH2120 are also greater than average. The crystal orientations sampled for WH833 (0.37 wt.% H$_2$O) are relatively deficient in directions normal to the c axis, and this may be responsible for some of the scatter in individual $C_{ij}$ (Fig. 4). Nevertheless, aggregate moduli obtained from the single-crystal elastic constants are likely well determined because trade-off errors tend to cancel during averaging (Zha et al., 1996).

Table 2

<table>
<thead>
<tr>
<th>H$_2$O (wt.%)</th>
<th>$K_{50}$ (GPa)</th>
<th>$G_0$ (GPa)</th>
<th>$V_p$ (km/s)</th>
<th>$V_s$ (km/s)</th>
</tr>
</thead>
<tbody>
<tr>
<td>an–hw $^a$</td>
<td>0</td>
<td>174(3)</td>
<td>114(1)</td>
<td>9.69(5)</td>
</tr>
<tr>
<td>an–hw $^b$</td>
<td>0</td>
<td>170(2)</td>
<td>115(2)</td>
<td>9.65(5)</td>
</tr>
<tr>
<td>WH833</td>
<td>0.37(4)</td>
<td>165.4(9)</td>
<td>108.6(6)</td>
<td>9.48(2)</td>
</tr>
<tr>
<td>WH2120</td>
<td>0.84(8)</td>
<td>160.3(7)</td>
<td>105.3(6)</td>
<td>9.36(2)</td>
</tr>
<tr>
<td>SS0401</td>
<td>1.66(17)</td>
<td>149.2(6)</td>
<td>98.6(4)</td>
<td>9.09(2)</td>
</tr>
</tbody>
</table>

$^a$ Sawamoto et al. (1984).

$^b$ Zha et al. (1997).
4. Discussion

4.1. Aggregate elastic moduli of hydrous wadsleyite

Table 2 shows the VRH (Voigt–Reuss–Hill) averages for the adiabatic elastic moduli of randomly oriented polycrystalline aggregates of hydrous wadsleyite. Also shown are VRH average compressional and shear wave velocities. The bulk modulus and shear modulus decrease linearly with water content (Fig. 5) and can be fitted by the equation:

\[
K_{S0} = 170.9(9) - 13.0(8) \times C_{H2O} \\
G_0 = 111.7(6) - 7.8(4) \times C_{H2O}
\]

where \(K_{S0}\) is the adiabatic bulk modulus in GPa, \(G_0\) is the shear modulus and \(C_{H2O}\) is the H2O weight percentage. As discussed previously, nominally anhydrous wadsleyite of previous studies may contain 50 ppm or more water by weight (Jacobsen et al., 2005). The extrapolated bulk modulus for anhydrous wadsleyite is in a good agreement with previous data (Sawamoto et al., 1984; Zha et al., 1997; Liu et al., 2005) (Fig. 5). The extrapolated shear modulus for anhydrous wadsleyite is consistent with or slightly lower than previous values (Sawamoto et al., 1984; Zha et al., 1997; Liu et al., 2005).

According to (4) and (5), 1 wt.% H2O corresponds to a 7.6% decrease in \(K_{S0}\) and a 7.0% decrease in \(G_0\). Using available data for other olivine polymorphs and assuming a linear relationship between aggregate elastic moduli and water content, the effect of H2O on olivine and ringwoodite can also be estimated. For hydrous olivine, 1 wt.% H2O would correspond to a 2.9% decrease in \(K_{S0}\) and a 1.6% decrease in \(G_0\) (Jacobsen et al., 2006). For hydrous ringwoodite, 1 wt.% H2O corresponds to a 4.7% (Wang et al., 2003) to 7.4% (Inoue et al., 1998) decrease in \(K_{S0}\) and a 5% decrease in \(G_0\) (Inoue et al., 1998; Wang et al., 2003). Thus, at least for Fe-free compositions, incorporation of water appears to have greater effect on the bulk and shear moduli of wadsleyite than for olivine and ringwoodite. For density, 1 wt.% H2O in wadsleyite leads to a 1.3% decrease in density.

The olivine to wadsleyite phase transition is generally accepted as the main source of the 410-km seismic discontinuity in the mantle. Seismic studies typically show about a 5–6% increase in density and a 4–6% increase in seismic velocity across this boundary (Dziewonski and Anderson, 1981; Grand and Helmberger, 1984; Mechie et al., 1993; Kennett et al., 1995). At ambient conditions, the velocity contrast between anhydrous olivine and wadsleyite is 12–13% (Sawamoto et al., 1984). If such a velocity contrast persisted to 410-km depth, the corresponding olivine fraction needed to produce a velocity jump that will match seismic data would be about ~40% (Sawamoto et al., 1984; Duffy et al., 1995). Petrological models of the mantle often favor an olivine-rich composition (~60 vol.%) mantle to satisfy seismic data. Gray lines show corresponding H2O contents of wadsleyite and olivine for different H2O partition coefficients, \(D_{H2O}^{wd\rightarrow ol}\).

Fig. 5. Adiabatic bulk and shear moduli as a function of H2O content. Solid circles and squares: this study; open circles and squares: for anhydrous wadsleyite (Sawamoto et al., 1984; Zha et al., 1997; Li et al., 2001); open upper triangles: isothermal bulk modulus of wadsleyite from Holl et al. (in press); open down triangles: Yusa and Inoue (1997). Solid line is a least-squares fit to the present data (dashed where extrapolated). Error bars are smaller than symbols when not shown.

Fig. 6. Contours of velocity contrast between wadsleyite and forsterite as a function of water content at ambient conditions. Dashed lines show a velocity contrast of 6.3–8.7% which is the range required for an olivine-rich (60 vol.%) mantle to satisfy seismic data. Gray lines show corresponding H2O contents of wadsleyite and olivine for different H2O partition coefficients, \(D_{H2O}^{wd\rightarrow ol}\).
Using our new elasticity data together with that of Jacobsen et al. (2006), we can now directly quantify the effect of H$_2$O on the velocity contrast between olivine and wadsleyite. Seismic velocities were calculated for the simple case of an Fe-free system at ambient conditions and the velocity contrast between olivine and wadsleyite is plotted as a function of water content in wadsleyite and olivine in Fig. 6. Results for compressional and shear waves are similar. The presence of 1.1–1.4 wt.% H$_2$O in wadsleyite can reduce the velocity contrast to 7–8% if olivine is anhydrous. Alternatively, if the H$_2$O content of olivine is 0.8 wt.%, then an H$_2$O content in wadsleyite of 1.3–1.8% is needed to reduce the velocity contrast to 7–8%. Recent studies have estimated that the wadsleyite/forsterite H$_2$O partition coefficient is in the range of 2–5 under mantle conditions (Chen et al., 2002; Hirschmann et al., 2005; Frost and Dolejš, 2007). Values of the velocity contrast between wadsleyite and olivine are indicated for this range of partitioning values in Fig. 6. If $D_{\text{H}_2\text{O}}^{\text{ol-wd}}$ = 5, then 1.1–1.4 wt.% H$_2$O in wadsleyite is needed to reduce the olivine/wadsleyite velocity contrast to below 8.3%. For $D_{\text{H}_2\text{O}}^{\text{ol-wd}}$ = 3, the corresponding amount of H$_2$O in wadsleyite is 1.2–1.5 wt.%. These water contents are close to or exceed the estimated storage capacity of the mantle at these depths (Demouchy et al., 2005), although the actual mantle water content may be less. These results indicate that the presence of H$_2$O can affect not only the thickness of the 410-km discontinuity (Chen et al., 2002; Hirschmann et al., 2005; Frost and Dolejš, 2007) but also the magnitude of the velocity change between the two phases. However, water contents must approach expected saturation values in order for the effects of water to reduce the velocity contrast at 410 km to the values required to match an olivine-rich (pyrolite) mantle.

4.2. Comparison with static compression data

The isothermal bulk modulus, $K_T$, was calculated from our measured adiabatic bulk modulus, $K_S$, using:

$$K_T = K_S/(1 + x\gamma T) \tag{6}$$

where $T$ is temperature, $\alpha$ is thermal expansion coefficient (Inoue et al., 2004) and $\gamma$ is the Gruneisen parameter (assumed to be identical to anhydrous wadsleyite (Chopelas, 1991)). The resulting $K_{T0}$ is listed in Table S3 and compared with previous static compression results.

The calculated $K_{T0}$ for 2.5 wt.% H$_2$O content extrapolated from this study is 13.3% lower than the value given by Yusa and Inoue (1997). For the 0.37 wt.% H$_2$O sample, the $K_{T0}$ estimated in this study is close to the value given by Holl et al. (in press) (fixed $K_{T0}$=4.0). But for the 1.66 wt.% H$_2$O sample, the $K_{T0}$ estimated in this study is 4.3% ($K_{T0}$=5.4(11)) or 8.5% (fixed $K_{T0}$=4.0) lower than the value given by Holl et al. (in press).

In static compression studies, there is a trade-off between the fitted isothermal bulk modulus $K_{T0}$ and its pressure derivative $K_{T0}'$. It is notable that other static compression studies on hydrous olivine polymorphs (Smyth et al., 2004, 2005; Manghani et al., 2005) suggest high H$_2$O contents lead to an increase of $K_{T0}$.

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**Fig. 7.** Equation of state of hydrous wadsleyite. Solid, dashed and dotted lines show fits with $V_0$, $K_{T0}$ constrained from X-ray and Brillouin data. Fitting results for $K_{T0}$ are given in Table S3. Static compression data for sample containing 2.5 wt.% H$_2$O are from Yusa and Inoue (1997); data for 0.37 wt.% and 1.66 wt.% H$_2$O are from Holl et al. (in press). Error bars are smaller than symbols when not shown.

**Fig. 8.** Birch plots showing variation of bulk and shear moduli as a function of density for olivine polymorphs from single-crystal elasticity data at ambient conditions. Solid down triangle: anhydrous olivine (Verma, 1960; Graham and Barsch, 1969; Kumazawa and Anderson, 1969; Ohno, 1976; Sumino et al., 1977; Sumino, 1979; Suzuki et al., 1983; Graham et al., 1988; Brown et al., 1989; Isaak et al., 1989; Webb, 1989; Isaak, 1992; Yoneda and Moriya, 1992; Zaug et al., 1993; Abramson et al., 1997; Spezziale et al., 2004); open down triangle: hydrous olivine (Jacobsen et al., 2006); solid square: anhydrous wadsleyite (Zha et al., 1993; Sumino, 1979; Suzuki et al., 1983; Graham et al., 1988; Isaak et al., 1989; Sumino et al., 1977); diamond: hydrous wadsleyite (this study); solid upper triangle: anhydrous ringwoodite (Weidner et al., 1984; Sinogeikin et al., 1997; Jackson et al., 2000; Sinogeikin et al., 2003); open upper triangle: hydrous ringwoodite (Inoue et al., 1998; Wang et al., 2003; Jacobsen et al., 2004; Jacobsen and Smyth, 2006); circle: chondrodite (Sinogeikin and Bass, 1999); open square: clinohumite (Fritz and Bass, 1997); short-dashed line and plus: polycrystalline ultrasonic data for anhydrous ringwoodite (Higo et al., 2006).
Using the third-order Birch–Murnaghan equation, we fitted equations of state for hydrous β-Mg2SiO4 with water content 0.37 wt.%, 0.84 wt.%, and 2.5 wt.% (Fig. 7). \( V_0 \) was directly determined by static compression studies (Yusa and Inoue, 1997; Holl et al., in press). \( K_T0 \) was calculated according to Eqs. (4) and (6) in this study. \( V_0 \) and \( K_T0 \) were fixed during the fitting. The results for \( K_T0 \) are given in Table S3, and the resulting compression curve is shown in Fig. 7. For the 0.37 wt.% H2O sample, \( K_T0 \) is close to 4 and consistent with static compression results (Holl et al., in press). For high water contents, incorporation of constraints from Brillouin data suggests \( K_T0 \) may be larger than 4. Direct measurements of elastic constants at high pressures are needed to test this hypothesis.

4.3. Bulk and shear moduli of minerals in the olivine system

Fig. 8 summarizes existing data on the bulk and shear moduli of olivine polymorphs as a function of density at ambient conditions. The figure focuses mainly on single-crystal data. The density increase for a given polymorph (solid lines in Fig. 8) reflects incorporation of iron along the solid solution. The shear modulus for all the three phases shows a monotonic decrease with density. The bulk modulus for both olivine and ringwoodite increases weakly with density following similar trends. However, the bulk modulus of wadsleyite decreases with density over the limited compositional range available. Also, the shear modulus of wadsleyite decreases more strongly with Fe than those of the other two polymorphs. Recent results from polycrystalline ultrasonics for elastic moduli of ringwoodite as a function of Fe content are also shown in the figure (short-dashed line) (Higo et al., 2006). The compositional trends differ from single-crystal data and the reasons for these differences need further investigation.

The figure also shows the variation of \( K_{S0} \) and \( G_0 \) across the three polymorphs for fixed composition (dashed lines). This is a demonstration of the validity of Birch’s law (Birch, 1961) for this system. The open symbols in Fig. 8 show the adiabatic bulk and shear moduli of hydrous olivine polymorphs as well as the minerals chondrodite and clinohumite. Incorporating water produces a change in density and mean atomic weight without a major structure change. It is clear from Fig. 8 that hydrous olivine polymorphs tend to follow the structural trend (dashed lines) indicated in the figure. That is, the effect of water incorporation is generally consistent with the predictions of Birch’s law for both the bulk and shear modulus.

5. Conclusions

The single-crystal elasticity of hydrous wadsleyite containing 0.37 wt.%, 0.84 wt.%, and 1.66 wt.% H2O were measured by Brillouin scattering at ambient conditions. All individual \( C_{ij} \) decrease approximately linearly as a function of water content. The bulk and shear moduli also decrease linearly with water content according to the relation (in GPa): \( K_{S0} = 170.9(9) - 13.0 \times 10^2 \), \( C_{ij} \) where \( C_{ij} \) is the H2O weight percentage. For Mg2SiO4 olivine polymorphs, incorporation 1 wt.% H2O in wadsleyite corresponds to a 7.6% reduction in \( K_{S0} \) and 7.0% reduction in \( G_0 \). The effect of water on the elasticity of wadsleyite is greater than for olivine and ringwoodite. Compressional, \( V_p \), and shear velocities, \( V_s \), of hydrous wadsleyite range from 9.48 to 9.09 km/s and 5.61 to 5.39 km/s, respectively for H2O content between 0.37 and 1.66 wt.%.

The contrast in compressional and shear wave velocity between wadsleyite and olivine was calculated as a function of H2O content at ambient conditions. Using an estimated H2O partition coefficient of 3, the velocity contrast between the two phases decreases from 12–13% under anhydrous conditions to 7–8% when wadsleyite contains 1.3–1.6 wt.% H2O for compressional velocity, and 1.6–1.9 wt.% H2O for shear velocity.

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Appendix A. Supplementary data

Supplementary data associated with this article can be found, in the online version, at doi:10.1016/j.epsl.2008.01.023.

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